



Topic/Skill	Definition/Tips	Example
1. Expression	A mathematical statement written using symbols, numbers or letters,	$3x + 2$ or $5y^2$
2. Equation	A statement showing that two expressions are equal	$2y - 17 = 15$
3. Identity	An equation that is true for all values of the variables An identity uses the symbol: \equiv	$2x \equiv x+x$
4. Formula	Shows the relationship between two or more variables	Area of a rectangle = length x width or $A = L \times W$
5. Simplifying Expressions	Collect 'like terms'. Be careful with negatives. x^2 and x are not like terms.	$2x + 3y + 4x - 5y + 3$ $= 6x - 2y + 3$ $3x + 4 - x^2 + 2x - 1 = 5x - x^2 + 3$
6. x times x	The answer is x^2 not $2x$.	Squaring is multiplying by itself, not by 2.
7. $p \times p \times p$	The answer is p^3 not $3p$	If $p=2$, then $p^3=2 \times 2 \times 2=8$, not $2 \times 3=6$
8. $p + p + p$	The answer is $3p$ not p^3	If $p=2$, then $2+2+2=6$, not $2^3 = 8$
9. Expand	To expand a bracket, multiply each term in the bracket by the expression outside the bracket.	$3(m + 7) = 3m + 21$
10. Factorise	The reverse of expanding. Factorising is writing an expression as a product of terms by ' taking out ' a common factor.	$6x - 15 = 3(2x - 5)$, where 3 is the common factor.



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1. Solve	To find the answer /value of something Use inverse operations on both sides of the equation (balancing method) until you find the value for the letter.	Solve $2x - 3 = 7$ Add 3 on both sides $2x = 10$ Divide by 2 on both sides $x = 5$
2. Inverse	Opposite	The inverse of addition is subtraction. The inverse of multiplication is division.
3. Rearranging Formulae	Use inverse operations on both sides of the formula (balancing method) until you find the expression for the letter.	Make x the subject of $y = \frac{2x-1}{z}$ Multiply both sides by z $yz = 2x - 1$ Add 1 to both sides $yz + 1 = 2x$ Divide by 2 on both sides $\frac{yz + 1}{2} = x$ We now have x as the subject.
4. Writing Formulae	Substitute letters for words in the question.	Bob charges £3 per window and a £5 call out charge. $C = 3N + 5$ Where N=number of windows and C=cost
5. Substitution	Replace letters with numbers. Be careful of $5x^2$. You need to square first, then multiply by 5.	$a = 3, b = 2$ and $c = 5$. Find: 1. $2a = 2 \times 3 = 6$ 2. $3a - 2b = 3 \times 3 - 2 \times 2 = 5$ 3. $7b^2 - 5 = 7 \times 2^2 - 5 = 23$

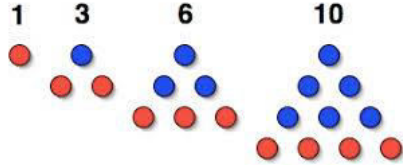


Topic/Skill	Definition/Tips	Example
1. Iteration	<p>The act of repeating a process over and over again, often with the aim of approximating a desired result more closely.</p> <p>Recursive Notation: $x_{n+1} = \sqrt{3x_n + 6}$</p>	$x_1 = 4$ $x_2 = \sqrt{3 \times 4 + 6} = 4.242640 \dots$ $x_3 = \sqrt{3 \times 4.242640 \dots + 6} = 4.357576 \dots$
2. Iterative Method	<p>To create an iterative formula, rearrange an equation with more than one x term to make one of the x terms the subject.</p> <p>You will be given the first value to substitute in, often called x_1.</p> <p>Keep substituting in your previous answer until your answers are the same to a certain degree of accuracy. This is called converging to a limit.</p> <p>Use the 'ANS' button on your calculator to keep substituting in the previous answer.</p>	<p>Use an iterative formula to find the positive root of $x^2 - 3x - 6 = 0$ to 3 decimal places.</p> <p>$x_1 = 4$</p> <p>Answer:</p> $x^2 = 3x + 6$ $x = \sqrt{3x + 6}$ <p>So $x_{n+1} = \sqrt{3x_n + 6}$</p> $x_1 = 4$ $x_2 = \sqrt{3 \times 4 + 6} = 4.242640 \dots$ $x_3 = \sqrt{3 \times 4.242640 \dots + 6} = 4.357576 \dots$ <p>Keep repeating...</p> $x_7 = 4.372068 \dots = 4.372 \text{ (3dp)}$ $x_8 = 4.372208 \dots = 4.372 \text{ (3dp)}$ <p>So answer is $x = 4.372 \text{ (3dp)}$</p>

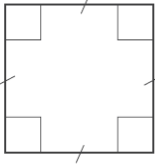
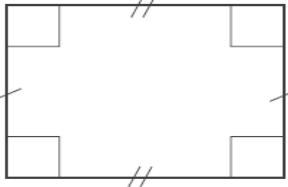
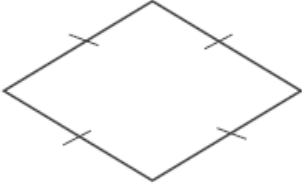
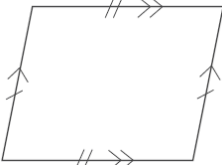
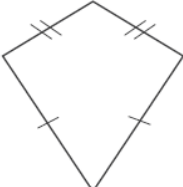
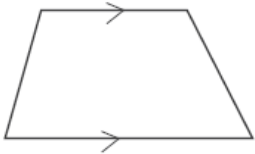


Topic/Skill	Definition/Tips	Example
1. Linear Sequence	A number pattern with a common difference .	2, 5, 8, 11... is a linear sequence
2. Term	Each value in a sequence is called a term.	In the sequence 2, 5, 8, 11..., 8 is the third term of the sequence.
3. Term-to-term rule	A rule which allows you to find the next term in a sequence if you know the previous term .	First term is 2. Term-to-term rule is 'add 3' Sequence is: 2, 5, 8, 11...
4. nth term	A rule which allows you to calculate the term that is in the nth position of the sequence. Also known as the 'position-to-term' rule. n refers to the position of a term in a sequence.	nth term is $3n - 1$ The 100 th term is $3 \times 100 - 1 = 299$
5. Finding the nth term of a linear sequence	1. Find the difference . 2. Multiply that by n . 3. Substitute $n = 1$ to find out what number you need to add or subtract to get the first number in the sequence .	Find the nth term of: 3, 7, 11, 15... 1. Difference is +4 2. Start with $4n$ 3. $4 \times 1 = 4$, so we need to subtract 1 to get 3. nth term = $4n - 1$
6. Fibonacci type sequences	A sequence where the next number is found by adding up the previous two terms	The Fibonacci sequence is: 1,1,2,3,5,8,13,21,34 ... An example of a Fibonacci-type sequence is: 4, 7, 11, 18, 29 ...
7. Geometric Sequence	A sequence of numbers where each term is found by multiplying the previous one by a number called the common ratio, r .	An example of a geometric sequence is: 2, 10, 50, 250 ... The common ratio is 5 Another example of a geometric sequence is: 81, -27, 9, -3, 1 ... The common ratio is $-\frac{1}{3}$
8. Quadratic Sequence	A sequence of numbers where the second difference is constant . A quadratic sequence will have a n^2 term.	 2 6 12 20 30 42 +4 +6 +8 +10 +12 +2 +2 +2 +2
9. nth term of a geometric sequence	ar^{n-1} where a is the first term and r is the common ratio	The nth term of 2, 10, 50, 250 Is $2 \times 5^{n-1}$


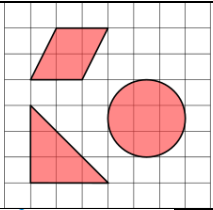

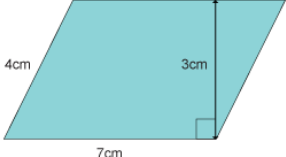
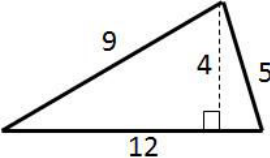
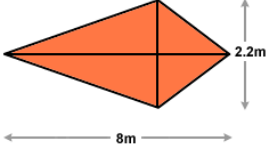
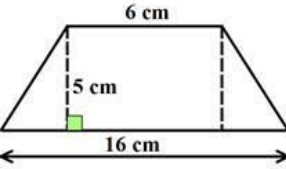
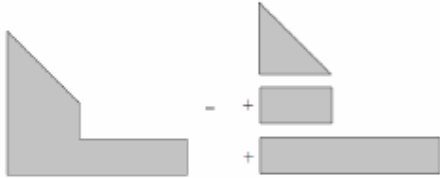


10. nth term of a quadratic sequence	<ol style="list-style-type: none">1. Find the first and second differences.2. Halve the second difference and multiply this by n^2.3. Substitute $n = 1, 2, 3, 4 \dots$ into your expression so far.4. Subtract this set of numbers from the corresponding terms in the sequence from the question.5. Find the nth term of this set of numbers.6. Combine the nth terms to find the overall nth term of the quadratic sequence. <p>Substitute values in to check your nth term works for the sequence.</p>	Find the nth term of: 4, 7, 14, 25, 40.. Answer: Second difference = +4 \rightarrow nth term = $2n^2$ Sequence: 4, 7, 14, 25, 40 $2n^2$ 2, 8, 18, 32, 50 Difference: 2, -1, -4, -7, -10 Nth term of this set of numbers is $-3n + 5$ Overall nth term: $2n^2 - 3n + 5$
11. Triangular numbers	The sequence which comes from a pattern of dots that form a triangle. 1, 3, 6, 10, 15, 21 ...	



Topic/Skill	Definition/Tips	Example
1. Square	<ul style="list-style-type: none"> • Four equal sides • Four right angles • Opposite sides parallel • Diagonals bisect each other at right angles • Four lines of symmetry • Rotational symmetry of order four 	
2. Rectangle	<ul style="list-style-type: none"> • Two pairs of equal sides • Four right angles • Opposite sides parallel • Diagonals bisect each other, not at right angles • Two lines of symmetry • Rotational symmetry of order two 	
3. Rhombus	<ul style="list-style-type: none"> • Four equal sides • Diagonally opposite angles are equal • Opposite sides parallel • Diagonals bisect each other at right angles • Two lines of symmetry • Rotational symmetry of order two 	
4. Parallelogram	<ul style="list-style-type: none"> • Two pairs of equal sides • Diagonally opposite angles are equal • Opposite sides parallel • Diagonals bisect each other, not at right angles • No lines of symmetry • Rotational symmetry of order two 	
5. Kite	<ul style="list-style-type: none"> • Two pairs of adjacent sides of equal length • One pair of diagonally opposite angles are equal (where different length sides meet) • Diagonals intersect at right angles, but do not bisect • One line of symmetry • No rotational symmetry 	
6. Trapezium	<ul style="list-style-type: none"> • One pair of parallel sides • No lines of symmetry • No rotational symmetry <p>Special Case: Isosceles Trapeziums have one line of symmetry.</p>	

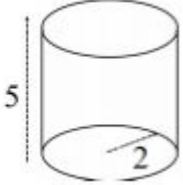
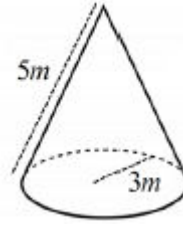


Topic/Skill	Definition/Tips	Example
1. Perimeter	The total distance around the outside of a shape. Units include: <i>mm, cm, m</i> etc.	<p>8 cm</p>  <p>5 cm</p> <p>$P = 8 + 5 + 8 + 5 = 26cm$</p>
2. Area	The amount of space inside a shape. Units include: mm^2, cm^2, m^2	
3. Area of a Rectangle	Length x Width	 <p>9 cm</p> <p>4 cm</p> <p>$A = 36cm^2$</p>
4. Area of a Parallelogram	Base x Perpendicular Height Not the slant height.	 <p>4cm</p> <p>7cm</p> <p>3cm</p> <p>$A = 21cm^2$</p>
5. Area of a Triangle	Base x Height ÷ 2	 <p>9</p> <p>4</p> <p>5</p> <p>12</p> <p>$A = 24cm^2$</p>
6. Area of a Kite	Split in to two triangles and use the method above.	 <p>2.2m</p> <p>8m</p> <p>$A = 8.8m^2$</p>
7. Area of a Trapezium	$\frac{(a + b)}{2} \times h$ <p>“Half the sum of the parallel side, times the height between them. That is how you calculate the area of a trapezium”</p>	 <p>6 cm</p> <p>5 cm</p> <p>16 cm</p> <p>$A = 55cm^2$</p>
8. Compound Shape	A shape made up of a combination of other known shapes put together.	

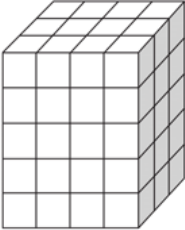
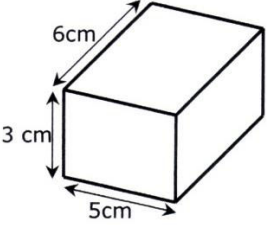
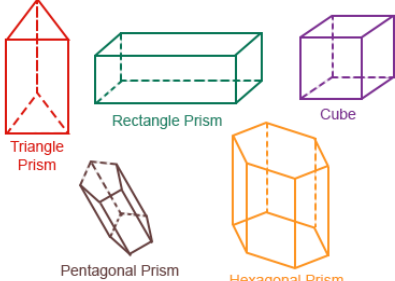
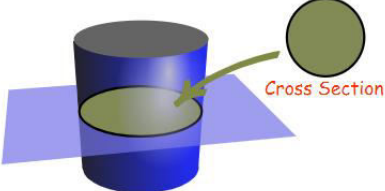
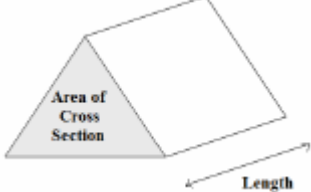
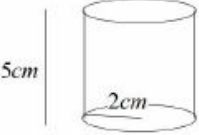
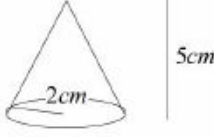


Topic/Skill	Definition/Tips	Example
1. Circle	A circle is the locus of all points equidistant from a central point.	
2. Parts of a Circle	<p>Radius – the distance from the centre of a circle to the edge</p> <p>Diameter – the total distance across the width of a circle through the centre.</p> <p>Circumference – the total distance around the outside of a circle</p> <p>Chord – a straight line whose end points lie on a circle</p> <p>Tangent – a straight line which touches a circle at exactly one point</p> <p>Arc – a part of the circumference of a circle</p> <p>Sector – the region of a circle enclosed by two radii and their intercepted arc</p> <p>Segment – the region bounded by a chord and the arc created by the chord</p>	<p style="text-align: center;">Parts of a Circle</p>
3. Area of a Circle	$A = \pi r^2$ which means ‘pi x radius squared’.	If the radius was 5cm, then: $A = \pi \times 5^2 = 78.5cm^2$
4. Circumference of a Circle	$C = \pi d$ which means ‘pi x diameter’	If the radius was 5cm, then: $C = \pi \times 10 = 31.4cm$
5. π (‘pi’)	Pi is the circumference of a circle divided by the diameter. $\pi \approx 3.14$	
6. Arc Length of a Sector	The arc length is part of the circumference. Take the angle given as a fraction over 360° and multiply by the circumference .	<p>Arc Length = $\frac{115}{360} \times \pi \times 8 = 8.03cm$</p>
7. Area of a Sector	The area of a sector is part of the total area. Take the angle given as a fraction over 360° and multiply by the area .	<p>Area = $\frac{115}{360} \times \pi \times 4^2 = 16.1cm^2$</p>

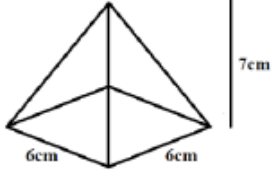
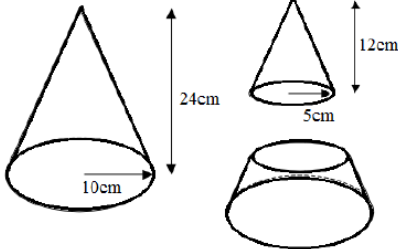


8. Surface Area of a Cylinder	Curved Surface Area = πdh or $2\pi rh$ Total SA = $2\pi r^2 + \pi dh$ or $2\pi r^2 + 2\pi rh$	 $Total SA = 2\pi(2)^2 + \pi(4)(5) = 28\pi$
9. Surface Area of a Cone	Curved Surface Area = πrl where $l = slant\ height$ Total SA = $\pi rl + \pi r^2$ You may need to use Pythagoras' Theorem to find the slant height	 $Total SA = \pi(3)(5) + \pi(3)^2 = 24\pi$
10. Surface Area of a Sphere	$SA = 4\pi r^2$ Look out for hemispheres – halve the SA of a sphere and add on a circle (πr^2)	Find the surface area of a sphere with radius 3cm. $SA = 4\pi(3)^2 = 36\pi cm^2$



Topic/Skill	Definition/Tips	Example
1. Volume	Volume is a measure of the amount of space inside a solid shape. Units: mm^3, cm^3, m^3 etc.	
2. Volume of a Cube/Cuboid	$V = \text{Length} \times \text{Width} \times \text{Height}$ $V = L \times W \times H$ You can also use the Volume of a Prism formula for a cube/cuboid.	 <p style="text-align: center;"> $\text{volume} = 6 \times 5 \times 3$ $= 90 \text{ cm}^3$ </p>
3. Prism	A prism is a 3D shape whose cross section is the same throughout.	
4. Cross Section	The cross section is the shape that continues all the way through the prism .	
5. Volume of a Prism	$V = \text{Area of Cross Section} \times \text{Length}$ $V = A \times L$	
6. Volume of a Cylinder	$V = \pi r^2 h$	 <p style="text-align: center;"> $V = \pi(4)(5)$ $= 62.8 \text{ cm}^3$ </p>
7. Volume of a Cone	$V = \frac{1}{3} \pi r^2 h$	 <p style="text-align: center;"> $V = \frac{1}{3} \pi(4)(5)$ $= 20.9 \text{ cm}^3$ </p>



8. Volume of a Pyramid	$\text{Volume} = \frac{1}{3}Bh$ where B = area of the base	 $V = \frac{1}{3} \times 6 \times 6 \times 7 = 84\text{cm}^3$
9. Volume of a Sphere	$V = \frac{4}{3}\pi r^3$ Look out for hemispheres – just halve the volume of a sphere.	Find the volume of a sphere with diameter 10cm. $V = \frac{4}{3}\pi(5)^3 = \frac{500\pi}{3}\text{cm}^3$
10. Frustums	A frustum is a solid (usually a cone or pyramid) with the top removed . Find the volume of the whole shape, then take away the volume of the small cone/pyramid removed at the top.	 Volume = ? $V = \frac{1}{3}\pi(10)^2(24) - \frac{1}{3}\pi(5)^2(12)$ $= 700\pi\text{cm}^3$