



| Topic/Skill           | Definition/Tips  | Example  |
|-----------------------|--|--|
| 1. Integer            | A <b>whole number</b> that can be positive, negative or zero.  | -3, 0, 92  |
| 2. Decimal            | A number with a <b>decimal point</b> in it. Can be positive or negative.   | 3.7, 0.94, -24.07  |
| 3. Negative Number    | A number that is <b>less than zero</b> . Can be decimals.  | -8, -2.5   |
| 4. Addition           | To find the <b>total</b> , or <b>sum</b> , of two or more numbers.<br><br>'add', 'plus', 'sum'   | $3 + 2 + 7 = 12$   |
| 5. Subtraction        | To find the <b>difference</b> between two numbers.<br>To find out how many are left when some are taken away.<br><br>'minus', 'take away', 'subtract'  | $10 - 3 = 7$   |
| 6. Multiplication     | Can be thought of as <b>repeated addition</b> .<br><br>'multiply', 'times', 'product'  | $3 \times 6 = 6 + 6 + 6 = 18$  |
| 7. Division           | Splitting into equal parts or groups.<br>The process of calculating the <b>number of times one number is contained within another one</b> .<br><br>'divide', 'share'   | $20 \div 4 = 5$<br><br>$\frac{20}{4} = 5$  |
| 8. Remainder          | The amount ' <b>left over</b> ' after dividing one integer by another.   | The remainder of $20 \div 6$ is 2, because 6 divides into 20 exactly 3 times, with 2 left over.  |
| 9. BIDMAS             | An acronym for the <b>order</b> you should do calculations in.<br><br>BIDMAS stands for ' <b>Brackets, Indices, Division, Multiplication, Addition and Subtraction</b> '.<br><br>Indices are also known as 'powers' or 'orders'.<br><br>With strings of division and multiplication, or strings of addition and subtraction, and no brackets, work from left to right. | $6 + 3 \times 5 = 21, \text{not } 45$<br><br>$5^2 = 25$ , where the 2 is the index/power.<br><br>$12 \div 4 \div 2 = 1.5, \text{not } 6$ |
| 10. Recurring Decimal | A decimal number that has <b>digits that repeat forever</b> .<br><br>The part that repeats is usually shown by placing a dot above the digit that repeats, or  | $\frac{1}{3} = 0.333 \dots = 0.\dot{3}$<br><br>$\frac{1}{7} = 0.142857142857 \dots = 0.\dot{1}4285\dot{7}$                               |



|  |  |  |
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|  | dots over the first and last digit of the repeating pattern. | $\frac{77}{600} = 0.128333 \dots = 0.128\dot{3}$ |
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|------------------------|--|---|
| 1. Place Value         | The <b>value</b> of where a <b>digit</b> is within a number.   | In 726, the value of the 2 is 20, as it is in the 'tens' column.  |
| 2. Place Value Columns | The names of the columns that <b>determine the value of each digit</b> .<br><br>The 'ones' column is also known as the 'units' column.   | <p>PLACE VALUE CHART</p> <p>Millions<br/>Hundred Thousands<br/>Ten Thousands<br/>Thousands<br/>Hundreds<br/>Tens<br/>Ones<br/>Decimal Point<br/>Tenths<br/>Hundredths<br/>Thousandths<br/>Ten-Thousandths<br/>Hundred-Thousandths<br/>Millionths</p>  |
| 3. Rounding            | To make a number simpler but keep its value close to what it was.<br><br>If the <b>digit to the right</b> of the rounding digit is <b>less than 5, round down</b> .<br>If the <b>digit to the right</b> of the rounding digit is <b>5 or more, round up</b> .                        | 74 rounded to the nearest ten is 70, because 74 is closer to 70 than 80.<br><br>152,879 rounded to the nearest thousand is 153,000.   |
| 4. Decimal Place       | The <b>position</b> of a digit to the <b>right of a decimal point</b> .  | In the number 0.372, the 7 is in the second decimal place.<br><br>0.372 rounded to two decimal places is 0.37, because the 2 tells us to round down.<br><br>Careful with money - don't write £27.4, instead write £27.40  |
| 5. Significant Figure  | The significant figures of a number are the digits which <b>carry meaning</b> (ie. are significant) to the size of the number.<br><br>The <b>first significant figure</b> of a number <b>cannot be zero</b> .<br><br>In a number with a decimal, trailing zeros are not significant. | In the number 0.00821, the first significant figure is the 8.<br><br>In the number 2.740, the 0 is not a significant figure.<br><br>0.00821 rounded to 2 significant figures is 0.0082.<br><br>19357 rounded to 3 significant figures is 19400. We need to include the two zeros at the end to keep the digits in the same place value columns. |
| 6. Truncation          | A method of approximating a decimal number by <b>dropping all decimal places</b> past a certain point <b>without rounding</b> .  | 3.14159265... can be truncated to 3.1415 (note that if it had been rounded, it would become 3.1416)   |
| 7. Error Interval      | A <b>range of values</b> that a number could have taken before being rounded or truncated.<br><br>An error interval is written using inequalities, with a <b>lower bound</b> and an <b>upper bound</b> .   | 0.6 has been rounded to 1 decimal place.<br><br>The error interval is:<br><br>$0.55 \leq x < 0.65$<br><br>The lower bound is 0.55<br>The upper bound is 0.65  |



|                               |  |   |
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|                               | Note that the lower bound inequality can be 'equal to', but the upper bound cannot be 'equal to'.  |   |
| 8. Estimate                   | To find something <b>close to the correct answer</b> .   | An estimate for the height of a man is 1.8 metres.  |
| 9. Approximation              | When using approximations to estimate the solution to a calculation, <b>round each number in the calculation to 1 significant figure</b> .<br><br>$\approx$ means 'approximately equal to' | $\frac{348 + 692}{0.526} \approx \frac{300 + 700}{0.5} = 2000$<br><br>'Note that dividing by 0.5 is the same as multiplying by 2'   |
| 10. Rational Number           | A number of the form $\frac{p}{q}$ , where <b>p and q are integers and <math>q \neq 0</math></b> .<br><br>A number that cannot be written in this form is called an 'irrational' number    | $\frac{4}{9}, 6, -\frac{1}{3}, \sqrt{25}$ are examples of rational numbers.<br><br>$\pi, \sqrt{2}$ are examples of an irrational numbers.   |
| 11. Surd                      | The <b>irrational number</b> that is a <b>root of a positive integer</b> , whose value cannot be determined exactly.<br><br>Surd have <b>infinite non-recurring decimals</b> .             | $\sqrt{2}$ is a surd because it is a root which cannot be determined exactly.<br><br>$\sqrt{2} = 1.41421356 \dots$ which never repeats.   |
| 12. Rules of Surds            | $\sqrt{ab} = \sqrt{a} \times \sqrt{b}$<br>$\sqrt{\frac{a}{b}} = \frac{\sqrt{a}}{\sqrt{b}}$<br>$a\sqrt{c} \pm b\sqrt{c} = (a \pm b)\sqrt{c}$<br>$\sqrt{a} \times \sqrt{a} = a$              | $\sqrt{48} = \sqrt{16} \times \sqrt{3} = 4\sqrt{3}$<br>$\sqrt{\frac{25}{36}} = \frac{\sqrt{25}}{\sqrt{36}} = \frac{5}{6}$<br>$2\sqrt{5} + 7\sqrt{5} = 9\sqrt{5}$<br>$\sqrt{7} \times \sqrt{7} = 7$  |
| 13. Rationalise a Denominator | The process of rewriting a fraction so that the <b>denominator contains only rational numbers</b> .  | $\frac{\sqrt{3}}{\sqrt{2}} = \frac{\sqrt{3} \times \sqrt{2}}{\sqrt{2} \times \sqrt{2}} = \frac{\sqrt{6}}{2}$<br>$\frac{6}{3 + \sqrt{7}} = \frac{6(3 - \sqrt{7})}{(3 + \sqrt{7})(3 - \sqrt{7})}$ $= \frac{18 - 6\sqrt{7}}{9 - 7}$ $= \frac{18 - 6\sqrt{7}}{2} = 9 - 3\sqrt{7}$ |



| Topic/Skill             | Definition/Tips  | Example   |
|-------------------------|--|---|
| 1. Solve                | To find the <b>answer</b> /value of something<br><br>Use <b>inverse operations</b> on both sides of the equation (balancing method) until you find the value for the letter. | Solve $2x - 3 = 7$<br><br>Add 3 on both sides<br>$2x = 10$<br>Divide by 2 on both sides<br>$x = 5$  |
| 2. Inverse              | <b>Opposite</b>  | The inverse of addition is subtraction.<br>The inverse of multiplication is division.   |
| 3. Rearranging Formulae | Use <b>inverse operations</b> on both sides of the formula (balancing method) until you find the expression for the letter.  | Make x the subject of $y = \frac{2x-1}{z}$<br><br>Multiply both sides by z<br>$yz = 2x - 1$<br>Add 1 to both sides<br>$yz + 1 = 2x$<br>Divide by 2 on both sides<br>$\frac{yz + 1}{2} = x$<br>We now have x as the subject. |
| 4. Writing Formulae     | <b>Substitute letters for words</b> in the question.   | Bob charges £3 per window and a £5 call out charge.<br><br>$C = 3N + 5$<br><br>Where N=number of windows and C=cost   |
| 5. Substitution         | <b>Replace letters with numbers.</b><br><br>Be careful of $5x^2$ . You need to square first, then multiply by 5.   | $a = 3, b = 2$ and $c = 5$ . Find:<br>1. $2a = 2 \times 3 = 6$<br>2. $3a - 2b = 3 \times 3 - 2 \times 2 = 5$<br>3. $7b^2 - 5 = 7 \times 2^2 - 5 = 23$   |



| Topic/Skill             | Definition/Tips   | Example  |
|-------------------------|---|--|
| 1. Expression           | A mathematical statement written using <b>symbols, numbers or letters,</b>  | $3x + 2$ or $5y^2$   |
| 2. Equation             | A statement showing that <b>two expressions are equal</b>   | $2y - 17 = 15$   |
| 3. Identity             | An equation that is <b>true for all values</b> of the variables<br><br>An identity uses the symbol: $\equiv$                | $2x \equiv x+x$  |
| 4. Formula              | Shows the <b>relationship</b> between <b>two or more variables</b>  | Area of a rectangle = length x width or $A = L \times W$   |
| 5. Coefficient          | A <b>number</b> used to <b>multiply</b> a <b>variable</b> .<br><br>It is the number that comes before/in front of a letter. | $6z$<br><br>6 is the coefficient<br>z is the variable  |
| 6. Odds and Evens       | An <b>even</b> number is a <b>multiple of 2</b><br>An <b>odd</b> number is an integer which is <b>not a multiple of 2</b> . | If n is an integer (whole number):<br><br>An even number can be represented by <b>2n</b> or <b>2m</b> etc.<br><br>An odd number can be represented by <b>2n-1</b> or <b>2n+1</b> or <b>2m+1</b> etc. |
| 7. Consecutive Integers | Whole numbers that follow each other in order.  | If n is an integer:<br><br><b>n, n+1, n+2</b> etc. are consecutive integers.   |
| 8. Square Terms         | A term that is produced by multiply another term by itself.   | If n is an integer:<br><br>$n^2, m^2$ etc. are square integers   |
| 9. Sum                  | The sum of two or more numbers is the value you get when you add them together.   | The sum of 4 and 6 is 10   |
| 10. Product             | The product of two or more numbers is the value you get when you multiply them together.                                    | The product of 4 and 6 is 24   |
| 11. Multiple            | To show that an expression is a <b>multiple</b> of a number, you need to show that you can <b>factor out the number</b> .   | $4n^2 + 8n - 12$ is a multiple of 4 because it can be written as:<br><br>$4(n^2 + 2n - 3)$   |



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|--------------|--|--|
| 1. Iteration | <p>The act of <b>repeating a process</b> over and over again, often with the aim of <b>approximating</b> a desired result more closely.</p> <p><b>Recursive Notation:</b> <math>x_{n+1} = \sqrt{3x_n + 6}</math></p> | $x_1 = 4$ $x_2 = \sqrt{3 \times 4 + 6} = 4.242640 \dots$ $x_3 = \sqrt{3 \times 4.242640 \dots + 6}$ $= 4.357576 \dots$ |




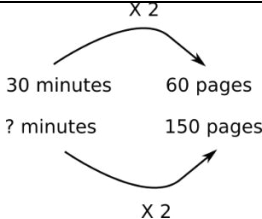
| Topic/Skill   | Definition/Tips   | Example   |
|---|---|---|
| 1. Algebraic Fraction                               | A fraction whose <b>numerator</b> and <b>denominator</b> are <b>algebraic expressions</b> .   | $\frac{6x}{3x - 1}$   |
| 2. Adding/<br>Subtracting<br>Algebraic<br>Fractions | For $\frac{a}{b} \pm \frac{c}{d}$ , the <b>common denominator</b> is $bd$<br><br>$\frac{a}{b} \pm \frac{c}{d} = \frac{ad}{bd} \pm \frac{bc}{bd} = \frac{ad \pm bc}{bd}$ | $\begin{aligned} & \frac{1}{x} + \frac{x}{2y} \\ &= \frac{1(2y)}{2xy} + \frac{x(x)}{2xy} \\ &= \frac{2y + x^2}{2xy} \end{aligned}$      |
| 3. Multiplying<br>Algebraic<br>Fractions            | <b>Multiply the numerators together</b> and the <b>denominators together</b> .<br><br>$\frac{a}{b} \times \frac{c}{d} = \frac{ac}{bd}$                                  | $\begin{aligned} & \frac{x}{3} \times \frac{x+2}{x-2} \\ &= \frac{x(x+2)}{3(x-2)} \\ &= \frac{x^2 + 2x}{3x - 6} \end{aligned}$          |
| 4. Dividing<br>Algebraic<br>Fractions               | <b>Multiply the first fraction by the reciprocal of the second fraction</b> .<br><br>$\frac{a}{b} \div \frac{c}{d} = \frac{a}{b} \times \frac{d}{c} = \frac{ad}{bc}$    | $\begin{aligned} & \frac{x}{3} \div \frac{2x}{7} \\ &= \frac{x}{3} \times \frac{7}{2x} \\ &= \frac{7x}{6x} = \frac{7}{6} \end{aligned}$ |
| 5. Simplifying<br>Algebraic<br>Fractions            | <b>Factorise</b> the numerator and denominator and <b>cancel common factors</b> .   | $\frac{x^2 + x - 6}{2x - 4} = \frac{(x + 3)(x - 2)}{2(x - 2)} = \frac{x + 3}{2}$  |




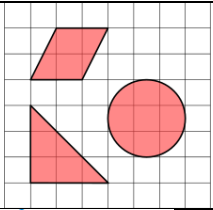

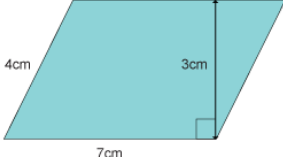
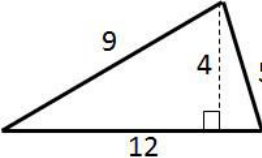
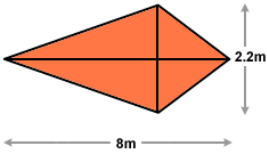
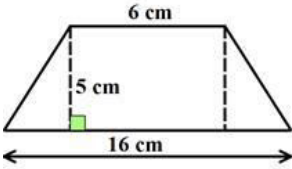
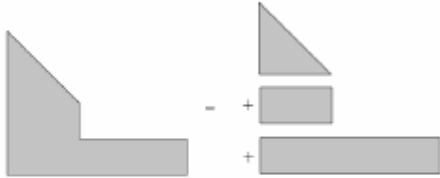


| <b>Topic/Skill</b>           | <b>Definition/Tips</b>   | <b>Example</b>  |
|------------------------------|--|---|
| 1. Metric System             | <p>A system of measures based on:</p> <ul style="list-style-type: none"> <li>- the metre for length</li> <li>- the kilogram for mass</li> <li>- the second for time</li> </ul> <p><b>Length: mm, cm, m, km</b><br/> <b>Mass: mg, g, kg</b><br/> <b>Volume: ml, cl, l</b></p> | <p><i>1 kilometre = 1000 metres</i><br/> <i>1 metre = 100 centimetres</i><br/> <i>1 centimetre = 10 millimetres</i></p> <p><i>1 kilogram = 1000 grams</i></p> |
| 2. Imperial System           | <p>A system of weights and measures originally developed in England, usually based on human quantities</p> <p><b>Length: inch, foot, yard, miles</b><br/> <b>Mass: lb, ounce, stone</b><br/> <b>Volume: pint, gallon</b></p>   | <p><i>1 lb = 16 ounces</i><br/> <i>1 foot = 12 inches</i><br/> <i>1 gallon = 8 pints</i></p>  |
| 3. Metric and Imperial Units | <p>Use the <b>unitary method</b> to convert between metric and imperial units.</p>   | <p><i>5 miles ≈ 8 kilometres</i><br/> <i>1 gallon ≈ 4.5 litres</i><br/> <i>2.2 pounds ≈ 1 kilogram</i><br/> <i>1 inch = 2.5 centimetres</i></p>               |

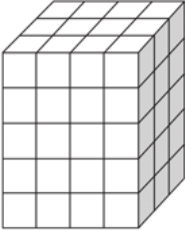
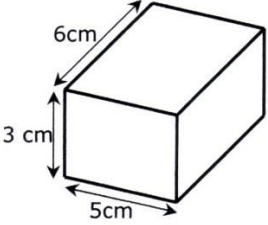
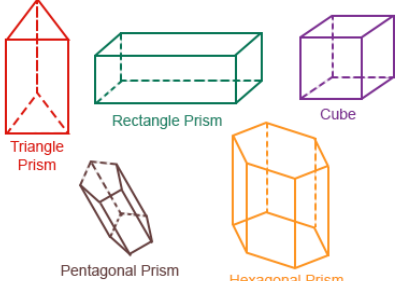
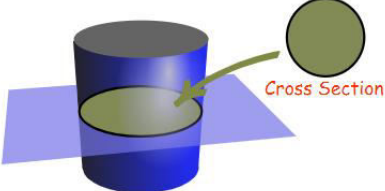
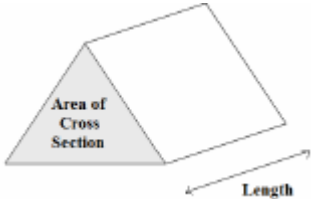
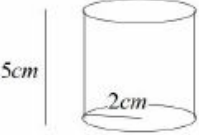
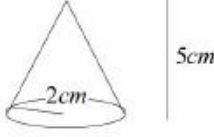


| Topic/Skill                          | Definition/Tips   | Example   |
|--------------------------------------|---|---|
| 1. Ratio                             | Ratio compares the size of <b>one part</b> to <b>another part</b> .<br><br>Written using the ':' symbol.  | $3 : 1$<br>  |
| 2. Proportion                        | Proportion compares the size of <b>one part</b> to the size of the <b>whole</b> .<br><br>Usually written as a fraction.   | In a class with 13 boys and 9 girls, the proportion of boys is $\frac{13}{22}$ and the proportion of girls is $\frac{9}{22}$  |
| 3. Simplifying Ratios                | <b>Divide</b> all parts of the ratio by a <b>common factor</b> .  | 5 : 10 = 1 : 2 (divide both by 5)<br>14 : 21 = 2 : 3 (divide both by 7)   |
| 4. Ratios in the form 1 : n or n : 1 | <b>Divide</b> both parts of the ratio by one of the numbers to make <b>one part equal 1</b> .   | $5 : 7 = 1 : \frac{7}{5}$ in the form 1 : n<br>$5 : 7 = \frac{5}{7} : 1$ in the form n : 1  |
| 5. Sharing in a Ratio                | <b>1. Add</b> the total parts of the ratio.<br><b>2. Divide</b> the amount to be shared by this value to find the value of one part.<br><b>3. Multiply</b> this value by each part of the ratio.<br><br>Use only if you <b>know the total</b> . | Share £60 in the ratio 3 : 2 : 1.<br><br>$3 + 2 + 1 = 6$<br>$60 \div 6 = 10$<br>$3 \times 10 = 30, 2 \times 10 = 20, 1 \times 10 = 10$<br>£30 : £20 : £10   |
| 6. Proportional Reasoning            | Comparing two things using <b>multiplicative reasoning</b> and applying this to a new situation.<br><br>Identify one multiplicative link and use this to find missing quantities.   |    |
| 7. Unitary Method                    | Finding the <b>value of a single unit</b> and then finding the necessary value by <b>multiplying</b> the single unit value.   | 3 cakes require 450g of sugar to make. Find how much sugar is needed to make 5 cakes.<br><br>3 cakes = 450g<br>So 1 cake = 150g (÷ by 3)<br>So 5 cakes = 750 g (x by 5)   |
| 8. Ratio already shared              | Find what <b>one part</b> of the ratio is worth using the <b>unitary method</b> .   | Money was shared in the ratio 3:2:5 between Ann, Bob and Cat. Given that Bob had £16, found out the total amount of money shared.<br><br>£16 = 2 parts<br>So £8 = 1 part<br>3 + 2 + 5 = 10 parts, so 8 x 10 = £80 |
| 9. Best Buys                         | Find the <b>unit cost</b> by <b>dividing the price by the quantity</b> .<br>The <b>lowest</b> number is the best value.   | 8 cakes for £1.28 → 16p each (÷ by 8)<br>13 cakes for £2.05 → 15.8p each (÷ by 13)<br>Pack of 13 cakes is best value.   |

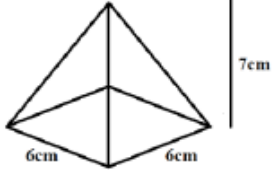
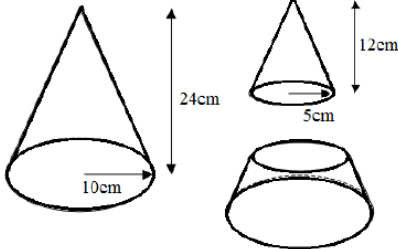


| Topic/Skill                | Definition/Tips   | Example  |
|----------------------------|---|--|
| 1. Perimeter               | The <b>total distance</b> around the <b>outside</b> of a shape.<br><br>Units include: <i>mm, cm, m</i> etc.   | <p>8 cm</p>  <p>5 cm</p> <p><math>P = 8 + 5 + 8 + 5 = 26cm</math></p> |
| 2. Area                    | The amount of <b>space inside</b> a shape.<br><br>Units include: $mm^2, cm^2, m^2$  |   |
| 3. Area of a Rectangle     | <b>Length x Width</b>   |  <p>9 cm</p> <p>4 cm</p> <p><math>A = 36cm^2</math></p>                |
| 4. Area of a Parallelogram | <b>Base x Perpendicular Height</b><br>Not the slant height.   |  <p>4cm</p> <p>7cm</p> <p>3cm</p> <p><math>A = 21cm^2</math></p>       |
| 5. Area of a Triangle      | <b>Base x Height ÷ 2</b>  |  <p>9</p> <p>4</p> <p>5</p> <p>12</p> <p><math>A = 24cm^2</math></p> |
| 6. Area of a Kite          | Split in to <b>two triangles</b> and use the method above.  |  <p>2.2m</p> <p>8m</p> <p><math>A = 8.8m^2</math></p>                |
| 7. Area of a Trapezium     | $\frac{(a + b)}{2} \times h$ <p>“Half the sum of the parallel side, times the height between them. That is how you calculate the area of a trapezium”</p> |  <p>6 cm</p> <p>5 cm</p> <p>16 cm</p> <p><math>A = 55cm^2</math></p> |
| 8. Compound Shape          | A shape made up of a <b>combination of other known shapes</b> put together.   |    |

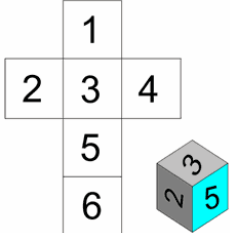
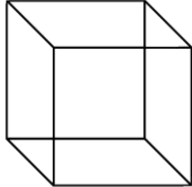
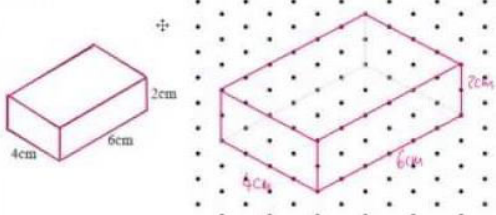


| Topic/Skill                | Definition/Tips  | Example   |
|----------------------------|--|---|
| 1. Volume                  | Volume is a measure of the amount of space inside a solid shape.<br><br>Units: $mm^3, cm^3, m^3$ etc.  |    |
| 2. Volume of a Cube/Cuboid | $V = \text{Length} \times \text{Width} \times \text{Height}$ $V = L \times W \times H$ You can also use the Volume of a Prism formula for a cube/cuboid. |  <p style="text-align: center;"> <math>\text{volume} = 6 \times 5 \times 3</math><br/> <math>= 90 \text{ cm}^3</math> </p> |
| 3. Prism                   | A prism is a 3D shape whose <b>cross section is the same</b> throughout.   |   |
| 4. Cross Section           | The <b>cross section</b> is the <b>shape that continues</b> all the way <b>through the prism</b> .   |    |
| 5. Volume of a Prism       | $V = \text{Area of Cross Section} \times \text{Length}$ $V = A \times L$   |    |
| 6. Volume of a Cylinder    | $V = \pi r^2 h$  |  <p style="text-align: center;"> <math>V = \pi(4)(5)</math><br/> <math>= 62.8 \text{ cm}^3</math> </p>                    |
| 7. Volume of a Cone        | $V = \frac{1}{3} \pi r^2 h$  |  <p style="text-align: center;"> <math>V = \frac{1}{3} \pi(4)(5)</math><br/> <math>= 20.9 \text{ cm}^3</math> </p>        |



|                        |   |   |
|------------------------|---|---|
| 8. Volume of a Pyramid | $\text{Volume} = \frac{1}{3}Bh$ where B = area of the base  |  $V = \frac{1}{3} \times 6 \times 6 \times 7 = 84\text{cm}^3$                                    |
| 9. Volume of a Sphere  | $V = \frac{4}{3}\pi r^3$<br>Look out for hemispheres – just halve the volume of a sphere.   | Find the volume of a sphere with diameter 10cm.<br>$V = \frac{4}{3}\pi(5)^3 = \frac{500\pi}{3}\text{cm}^3$  |
| 10. Frustums           | A frustum is a solid (usually a cone or pyramid) with the <b>top removed</b> .<br><br>Find the volume of the whole shape, then take away the volume of the small cone/pyramid removed at the top. | <br>Volume = ?<br>$V = \frac{1}{3}\pi(10)^2(24) - \frac{1}{3}\pi(5)^2(12)$ $= 700\pi\text{cm}^3$ |

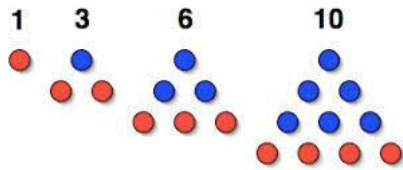


| Topic/Skill             | Definition/Tips  | Example   |
|-------------------------|--|---|
| 1. Net                  | A pattern that you can <b>cut and fold</b> to make a <b>model</b> of a <b>3D shape</b> .   |    |
| 2. Properties of Solids | <b>Faces = flat surfaces</b><br><b>Edges = sides/lengths</b><br><b>Vertices = corners</b>  | <p>A cube has 6 faces, 12 edges and 8 vertices.</p>  |
| 3. Plans and Elevations | <p>This takes 3D drawings and produces 2D drawings.</p> <p><b>Plan View:</b> from <b>above</b><br/> <b>Side Elevation:</b> from the <b>side</b><br/> <b>Front Elevation:</b> from the <b>front</b></p> |   |
| 4. Isometric Drawing    | A method for visually <b>representing 3D objects in 2D</b> .   |   |



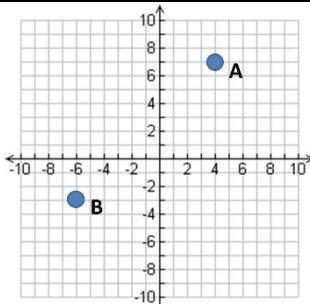
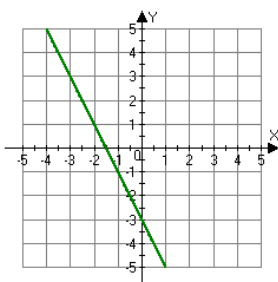
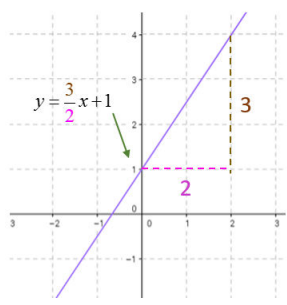
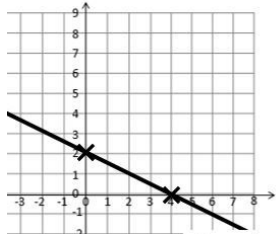
| Topic/Skill                                  | Definition/Tips   | Example   |
|--|---|---|
| 1. Linear Sequence                           | A number pattern with a <b>common difference</b> .  | 2, 5, 8, 11... is a linear sequence   |
| 2. Term                                      | <b>Each value</b> in a sequence is called a term.   | In the sequence 2, 5, 8, 11..., 8 is the third term of the sequence.  |
| 3. Term-to-term rule                         | A rule which allows you to <b>find the next term</b> in a sequence if you <b>know the previous term</b> .   | First term is 2. Term-to-term rule is 'add 3'<br><br>Sequence is: 2, 5, 8, 11...  |
| 4. nth term                                  | A rule which allows you to <b>calculate the term</b> that is in the <b>nth position</b> of the sequence.<br><br>Also known as the 'position-to-term' rule.<br><br><b>n</b> refers to the <b>position</b> of a term in a sequence. | nth term is $3n - 1$<br><br>The 100 <sup>th</sup> term is $3 \times 100 - 1 = 299$  |
| 5. Finding the nth term of a linear sequence | 1. Find the <b>difference</b> .<br>2. <b>Multiply that by n</b> .<br>3. Substitute $n = 1$ to <b>find out what number you need to add or subtract to get the first number in the sequence</b> .                                   | Find the nth term of: 3, 7, 11, 15...<br><br>1. Difference is +4<br>2. Start with $4n$<br>3. $4 \times 1 = 4$ , so we need to subtract 1 to get 3.<br>nth term = $4n - 1$                               |
| 6. Fibonacci type sequences                  | A sequence where the next number is found by <b>adding up the previous two terms</b>  | The Fibonacci sequence is:<br>1,1,2,3,5,8,13,21,34 ...<br><br>An example of a Fibonacci-type sequence is:<br>4, 7, 11, 18, 29 ...   |
| 7. Geometric Sequence                        | A sequence of numbers where each term is found by <b>multiplying the previous one</b> by a number called the <b>common ratio, r</b> .   | An example of a geometric sequence is:<br>2, 10, 50, 250 ...<br>The common ratio is 5<br><br>Another example of a geometric sequence is:<br>81, -27, 9, -3, 1 ...<br>The common ratio is $-\frac{1}{3}$ |
| 8. Quadratic Sequence                        | A sequence of numbers where the <b>second difference is constant</b> .<br><br>A quadratic sequence will have a $n^2$ term.  | <br>2      6      12      20      30      42<br>+4    +6    +8    +10   +12<br>+2    +2    +2    +2   |
| 9. nth term of a geometric sequence          | $ar^{n-1}$<br><br>where $a$ is the first term and $r$ is the common ratio   | The nth term of 2, 10, 50, 250 ... Is<br><br>$2 \times 5^{n-1}$   |



|                                      |   |   |
|--------------------------------------|---|---|
| 10. nth term of a quadratic sequence | <ol style="list-style-type: none"><li>1. Find the first and second differences.</li><li>2. Halve the second difference and multiply this by <math>n^2</math>.</li><li>3. Substitute <math>n = 1, 2, 3, 4 \dots</math> into your expression so far.</li><li>4. Subtract this set of numbers from the corresponding terms in the sequence from the question.</li><li>5. Find the nth term of this set of numbers.</li><li>6. Combine the nth terms to find the overall nth term of the quadratic sequence.</li></ol> <p>Substitute values in to check your nth term works for the sequence.</p> | Find the nth term of: 4, 7, 14, 25, 40..<br><br>Answer:<br>Second difference = +4 $\rightarrow$ nth term = $2n^2$<br><br>Sequence: 4, 7, 14, 25, 40<br>$2n^2$ 2, 8, 18, 32, 50<br>Difference: 2, -1, -4, -7, -10<br><br>Nth term of this set of numbers is $-3n + 5$<br><br>Overall nth term: $2n^2 - 3n + 5$ |
| 11. Triangular numbers               | The sequence which comes from a pattern of dots that form a triangle.<br><br>1, 3, 6, 10, 15, 21 ...  |    |

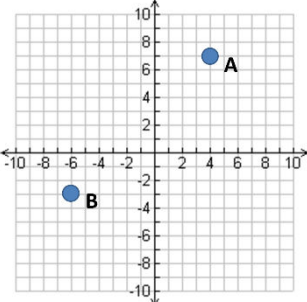
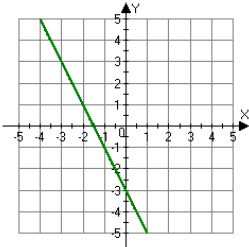
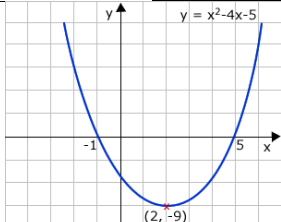




| Topic/Skill               | Definition/Tips   | Example   |    |    |    |    |   |   |   |   |           |   |   |   |   |   |   |   |
|---------------------------|---|---|----|----|----|----|---|---|---|---|-----------|---|---|---|---|---|---|---|
| 1. Coordinates            | Written in <b>pairs</b> . The <b>first</b> term is the <b>x-coordinate</b> (movement <b>across</b> ). The <b>second</b> term is the <b>y-coordinate</b> (movement <b>up or down</b> )   |  <div style="display: inline-block; vertical-align: top; margin-left: 20px;"> <p>A: (4,7)<br/>B: (-6,-3)</p> </div>   |    |    |    |    |   |   |   |   |           |   |   |   |   |   |   |   |
| 2. Midpoint of a Line     | <p>Method 1: <b>add the x coordinates and divide by 2, add the y coordinates and divide by 2</b></p> <p>Method 2: Sketch the line and find the values half way between the two x and two y values.</p>  | <p>Find the midpoint between (2,1) and (6,9)</p> $\frac{2+6}{2} = 4 \text{ and } \frac{1+9}{2} = 5$ <p>So, the midpoint is (4,5)</p>  |    |    |    |    |   |   |   |   |           |   |   |   |   |   |   |   |
| 3. Linear Graph           | <p><b>Straight line</b> graph.</p> <p>The general equation of a linear graph is <math>y = mx + c</math></p> <p>where <b>m</b> is the <b>gradient</b> and <b>c</b> is the <b>y-intercept</b>.</p> <p>The <b>equation</b> of a linear graph can contain an <b>x-term</b>, a <b>y-term</b> and a <b>number</b>.</p>  | <p>Example:</p>  <div style="display: inline-block; vertical-align: top; margin-left: 20px;"> <p>Other examples:<br/> <math>x = y</math><br/> <math>y = 4</math><br/> <math>x = -2</math><br/> <math>y = 2x - 7</math><br/> <math>y + x = 10</math><br/> <math>2y - 4x = 12</math></p> </div>  |    |    |    |    |   |   |   |   |           |   |   |   |   |   |   |   |
| 4. Plotting Linear Graphs | <p>Method 1: <b>Table of Values</b><br/>Construct a table of values to calculate coordinates.</p> <p>Method 2: <b>Gradient-Intercept Method</b> (use when the equation is in the form <math>y = mx + c</math>)</p> <ol style="list-style-type: none"> <li>Plots the y-intercept</li> <li>Using the gradient, plot a second point.</li> <li>Draw a line through the two points plotted.</li> </ol> <p>Method 3: <b>Cover-Up Method</b> (use when the equation is in the form <math>ax + by = c</math>)</p> <ol style="list-style-type: none"> <li>Cover the x term and solve the resulting equation. Plot this on the x – axis.</li> <li>Cover the y term and solve the resulting equation. Plot this on the y – axis.</li> <li>Draw a line through the two points plotted.</li> </ol> | <table border="1" style="margin-bottom: 20px; width: 100%; text-align: center;"> <tr style="background-color: #FFD700;"> <th>x</th> <td>-3</td> <td>-2</td> <td>-1</td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> </tr> <tr style="background-color: #FFD700;"> <th>y = x + 3</th> <td>0</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> </tr> </table>   | x  | -3 | -2 | -1 | 0 | 1 | 2 | 3 | y = x + 3 | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
| x                         | -3  | -2  | -1 | 0  | 1  | 2  | 3 |   |   |   |           |   |   |   |   |   |   |   |
| y = x + 3                 | 0   | 1   | 2  | 3  | 4  | 5  | 6 |   |   |   |           |   |   |   |   |   |   |   |

# Topic: Graphs and Graph Transformations



| Topic/Skill        | Definition/Tips   | Example   |
|--------------------|---|---|
| 1. Coordinates     | Written in <b>pairs</b> . The <b>first</b> term is the <b>x-coordinate</b> (movement <b>across</b> ). The <b>second</b> term is the <b>y-coordinate</b> (movement <b>up or down</b> )                           |  <p style="margin-left: 100px;">A: (4,7)<br/>B: (-6,-3)</p>   |
| 2. Linear Graph    | <b>Straight line</b> graph.<br>The <b>equation</b> of a linear graph can contain an <b>x-term</b> , a <b>y-term</b> and a <b>number</b> .   | <p>Example:</p>  <p style="margin-left: 100px;">Other examples:<br/> <math>x = y</math><br/> <math>y = 4</math><br/> <math>x = -2</math><br/> <math>y = 2x - 7</math><br/> <math>y + x = 10</math><br/> <math>2y - 4x = 12</math></p> |
| 3. Quadratic Graph | A ' <b>U-shaped</b> ' curve called a <b>parabola</b> .<br>The equation is of the form $y = ax^2 + bx + c$ , where $a, b$ and $c$ are numbers, $a \neq 0$ .<br>If $a < 0$ , the parabola is <b>upside down</b> . |  <p style="margin-left: 100px;"><math>y = x^2 - 4x - 5</math></p>   |