



Topic/Skill	Definition/Tips	Example
1. Square Number	The number you get when you multiply a number by itself .	1, 4, 9, 16, 25, 36, 49, 64, 81, 100, 121, 144, 169, 196, 225... $9^2 = 9 \times 9 = 81$
2. Square Root	The number you multiply by itself to get another number. The reverse process of squaring a number.	$\sqrt{36} = 6$ because $6 \times 6 = 36$
3. Solutions to $x^2 = \dots$	Equations involving squares have two solutions , one positive and one negative .	Solve $x^2 = 25$ $x = 5$ or $x = -5$ This can also be written as $x = \pm 5$
4. Cube Number	The number you get when you multiply a number by itself and itself again .	1, 8, 27, 64, 125... $2^3 = 2 \times 2 \times 2 = 8$
5. Cube Root	The number you multiply by itself and itself again to get another number. The reverse process of cubing a number.	$\sqrt[3]{125} = 5$ because $5 \times 5 \times 5 = 125$
6. Powers of...	The powers of a number are that number raised to various powers .	The powers of 3 are: $3^1 = 3$ $3^2 = 9$ $3^3 = 27$ $3^4 = 81$ etc.
7. Multiplication Index Law	When multiplying with the same base (number or letter), add the powers . $a^m \times a^n = a^{m+n}$	$7^5 \times 7^3 = 7^8$ $a^{12} \times a = a^{13}$ $4x^5 \times 2x^8 = 8x^{13}$
8. Division Index Law	When dividing with the same base (number or letter), subtract the powers . $a^m \div a^n = a^{m-n}$	$15^7 \div 15^4 = 15^3$ $x^9 \div x^2 = x^7$ $20a^{11} \div 5a^3 = 4a^8$
9. Brackets Index Laws	When raising a power to another power, multiply the powers together. $(a^m)^n = a^{mn}$	$(y^2)^5 = y^{10}$ $(6^3)^4 = 6^{12}$ $(5x^6)^3 = 125x^{18}$
10. Notable Powers	$p = p^1$ $p^0 = 1$	$99999^0 = 1$
11. Negative Powers	A negative power performs the reciprocal. $a^{-m} = \frac{1}{a^m}$	$3^{-2} = \frac{1}{3^2} = \frac{1}{9}$
12. Fractional Powers	The denominator of a fractional power acts as a 'root'. The numerator of a fractional power acts as a normal power. $a^{\frac{m}{n}} = (\sqrt[n]{a})^m$	$27^{\frac{2}{3}} = (\sqrt[3]{27})^2 = 3^2 = 9$ $\left(\frac{25}{16}\right)^{\frac{3}{2}} = \left(\frac{\sqrt{25}}{\sqrt{16}}\right)^3 = \left(\frac{5}{4}\right)^3 = \frac{125}{64}$





Topic/Skill	Definition/Tips	Example
1. Place Value	The value of where a digit is within a number.	In 726, the value of the 2 is 20, as it is in the 'tens' column.
2. Place Value Columns	The names of the columns that determine the value of each digit . The 'ones' column is also known as the 'units' column.	<p>PLACE VALUE CHART</p> <p>Millions Hundred Thousands Ten Thousands Thousands Hundreds Tens Ones Decimal Point Tenths Hundredths Thousandths Ten-Thousandths Hundred-Thousandths Millionths</p>
3. Rounding	To make a number simpler but keep its value close to what it was. If the digit to the right of the rounding digit is less than 5, round down . If the digit to the right of the rounding digit is 5 or more, round up .	74 rounded to the nearest ten is 70, because 74 is closer to 70 than 80. 152,879 rounded to the nearest thousand is 153,000.
4. Decimal Place	The position of a digit to the right of a decimal point .	In the number 0.372, the 7 is in the second decimal place. 0.372 rounded to two decimal places is 0.37, because the 2 tells us to round down. Careful with money - don't write £27.4, instead write £27.40
5. Significant Figure	The significant figures of a number are the digits which carry meaning (ie. are significant) to the size of the number. The first significant figure of a number cannot be zero . In a number with a decimal, trailing zeros are not significant.	In the number 0.00821, the first significant figure is the 8. In the number 2.740, the 0 is not a significant figure. 0.00821 rounded to 2 significant figures is 0.0082. 19357 rounded to 3 significant figures is 19400. We need to include the two zeros at the end to keep the digits in the same place value columns.
6. Truncation	A method of approximating a decimal number by dropping all decimal places past a certain point without rounding .	3.14159265... can be truncated to 3.1415 (note that if it had been rounded, it would become 3.1416)
7. Error Interval	A range of values that a number could have taken before being rounded or truncated. An error interval is written using inequalities, with a lower bound and an upper bound . Note that the lower bound inequality can be 'equal to', but the upper bound cannot be	0.6 has been rounded to 1 decimal place. The error interval is: $0.55 \leq x < 0.65$ The lower bound is 0.55 The upper bound is 0.65



	'equal to'.	
8. Estimate	To find something close to the correct answer .	An estimate for the height of a man is 1.8 metres.
9. Approximation	When using approximations to estimate the solution to a calculation, round each number in the calculation to 1 significant figure . \approx means 'approximately equal to'	$\frac{348 + 692}{0.526} \approx \frac{300 + 700}{0.5} = 2000$ 'Note that dividing by 0.5 is the same as multiplying by 2'



Topic/Skill	Definition/Tips	Example
1. Standard Form	$A \times 10^b$ <p>where $1 \leq A < 10$, $b = \text{integer}$</p>	$8400 = 8.4 \times 10^3$ $0.00036 = 3.6 \times 10^{-4}$
2. Multiplying or Dividing with Standard Form	<p>Multiply: Multiply the numbers and add the powers.</p> <p>Divide: Divide the numbers and subtract the powers.</p>	$(1.2 \times 10^3) \times (4 \times 10^6) = 8.8 \times 10^9$ $(4.5 \times 10^5) \div (3 \times 10^2) = 1.5 \times 10^3$
3. Adding or Subtracting with Standard Form	Convert in to ordinary numbers, calculate and then convert back in to standard form	$2.7 \times 10^4 + 4.6 \times 10^3$ $= 27000 + 4600 = 31600$ $= 3.16 \times 10^4$



Topic/Skill	Definition/Tips	Example
1. Expression	A mathematical statement written using symbols, numbers or letters,	$3x + 2$ or $5y^2$
2. Equation	A statement showing that two expressions are equal	$2y - 17 = 15$
3. Identity	An equation that is true for all values of the variables An identity uses the symbol: \equiv	$2x \equiv x+x$
4. Formula	Shows the relationship between two or more variables	Area of a rectangle = length x width or $A = L \times W$
5. Simplifying Expressions	Collect 'like terms'. Be careful with negatives. x^2 and x are not like terms.	$2x + 3y + 4x - 5y + 3$ $= 6x - 2y + 3$ $3x + 4 - x^2 + 2x - 1 = 5x - x^2 + 3$
6. x times x	The answer is x^2 not $2x$.	Squaring is multiplying by itself, not by 2.
7. $p \times p \times p$	The answer is p^3 not $3p$	If $p=2$, then $p^3=2 \times 2 \times 2=8$, not $2 \times 3=6$
8. $p + p + p$	The answer is $3p$ not p^3	If $p=2$, then $2+2+2=6$, not $2^3 = 8$
9. Expand	To expand a bracket, multiply each term in the bracket by the expression outside the bracket.	$3(m + 7) = 3m + 21$
10. Expanding double brackets	To expand a double bracket, multiply the first term in the first bracket by the expression inside the second bracket , then repeat for the second term in the first bracket (multiplying by the terms in the second bracket), then simplify.	$(n+5)(n-2) = n^2 - 2n + 5n - 10$ $= n^2 + 3n - 10$
11. Factorise	The reverse of expanding . Factorising is writing an expression as a product of terms by 'taking out' a common factor .	$6x - 15 = 3(2x - 5)$, where 3 is the common factor.



Topic/Skill	Definition/Tips	Example
1. Solve	To find the answer /value of something Use inverse operations on both sides of the equation (balancing method) until you find the value for the letter.	Solve $2x - 3 = 7$ Add 3 on both sides $2x = 10$ Divide by 2 on both sides $x = 5$
2. Inverse	Opposite	The inverse of addition is subtraction. The inverse of multiplication is division.
3. Rearranging Formulae	Use inverse operations on both sides of the formula (balancing method) until you find the expression for the letter.	Make x the subject of $y = \frac{2x-1}{z}$ Multiply both sides by z $yz = 2x - 1$ Add 1 to both sides $yz + 1 = 2x$ Divide by 2 on both sides $\frac{yz + 1}{2} = x$ We now have x as the subject.
4. Writing Formulae	Substitute letters for words in the question.	Bob charges £3 per window and a £5 call out charge. $C = 3N + 5$ Where N=number of windows and C=cost
5. Substitution	Replace letters with numbers. Be careful of $5x^2$. You need to square first, then multiply by 5.	$a = 3, b = 2$ and $c = 5$. Find: 1. $2a = 2 \times 3 = 6$ 2. $3a - 2b = 3 \times 3 - 2 \times 2 = 5$ 3. $7b^2 - 5 = 7 \times 2^2 - 5 = 23$



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1. Types of Data	<p>Qualitative Data – non-numerical data</p> <p>Quantitative Data – numerical data</p> <p>Continuous Data – data that can take any numerical value within a given range.</p> <p>Discrete Data – data that can take only specific values within a given range.</p>	<p>Qualitative Data – eye colour, gender etc.</p> <p>Continuous Data – weight, voltage etc.</p> <p>Discrete Data – number of children, shoe size etc.</p>																				
2. Grouped Data	<p>Data that has been bundled in to categories.</p> <p>Seen in grouped frequency tables, histograms, cumulative frequency etc.</p>	<table border="1"> <thead> <tr> <th>Foot length, l, (cm)</th> <th>Number of children</th> </tr> </thead> <tbody> <tr> <td>$10 \leq l < 12$</td> <td>5</td> </tr> <tr> <td>$12 \leq l < 17$</td> <td>53</td> </tr> </tbody> </table>	Foot length, l , (cm)	Number of children	$10 \leq l < 12$	5	$12 \leq l < 17$	53														
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3. Primary /Secondary Data	<p>Primary Data – collected yourself for a specific purpose.</p> <p>Secondary Data – collected by someone else for another purpose.</p>	<p>Primary Data – data collected by a student for their own research project.</p> <p>Secondary Data – Census data used to analyse link between education and earnings.</p>																				
4. Mean	<p>Add up the values and divide by how many values there are.</p>	<p>The mean of 3, 4, 7, 6, 0, 4, 6 is</p> $\frac{3 + 4 + 7 + 6 + 0 + 4 + 6}{7} = 5$																				
5. Mean from a Table	<ol style="list-style-type: none"> Find the midpoints (if necessary) Multiply Frequency by values or midpoints Add up these values Divide this total by the Total Frequency <p>If grouped data is used, the answer will be an estimate.</p>	<table border="1"> <thead> <tr> <th>Height in cm</th> <th>Frequency</th> <th>Midpoint</th> <th>F × M</th> </tr> </thead> <tbody> <tr> <td>$0 < h \leq 10$</td> <td>8</td> <td>5</td> <td>$8 \times 5 = 40$</td> </tr> <tr> <td>$10 < h \leq 30$</td> <td>10</td> <td>20</td> <td>$10 \times 20 = 200$</td> </tr> <tr> <td>$30 < h \leq 40$</td> <td>6</td> <td>35</td> <td>$6 \times 35 = 210$</td> </tr> <tr> <td>Total</td> <td>24</td> <td>Ignore!</td> <td>450</td> </tr> </tbody> </table> <p>Estimated Mean height: $450 \div 24 = 18.75\text{cm}$</p>	Height in cm	Frequency	Midpoint	F × M	$0 < h \leq 10$	8	5	$8 \times 5 = 40$	$10 < h \leq 30$	10	20	$10 \times 20 = 200$	$30 < h \leq 40$	6	35	$6 \times 35 = 210$	Total	24	Ignore!	450
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6. Median Value	<p>The middle value.</p> <p>Put the data in order and find the middle one.</p> <p>If there are two middle values, find the number half way between them by adding them together and dividing by 2.</p>	<p>Find the median of: 4, 5, 2, 3, 6, 7, 6</p> <p>Ordered: 2, 3, 4, 5, 6, 6, 7</p> <p>Median = 5</p>																				
7. Median from a Table	<p>Use the formula $\frac{(n+1)}{2}$ to find the position of the median.</p> <p>n is the total frequency.</p>	<p>If the total frequency is 15, the median will be the $\left(\frac{15+1}{2}\right) = 8\text{th}$ position</p>																				
8. Mode /Modal Value	<p>Most frequent/common.</p> <p>Can have more than one mode (called bi-modal or multi-modal) or no mode (if all values appear once)</p>	<p>Find the mode: 4, 5, 2, 3, 6, 4, 7, 8, 4</p> <p>Mode = 4</p>																				
9. Range	<p>Highest value subtract the Smallest value</p> <p>Range is a ‘measure of spread’. The smaller</p>	<p>Find the range: 3, 31, 26, 102, 37, 97.</p> <p>Range = $102 - 3 = 99$</p>																				

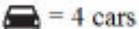
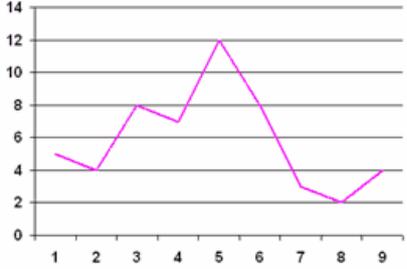


	the range the more <u>consistent</u> the data.																							
10. Outlier	A value that 'lies outside' most of the other values in a set of data. An outlier is much smaller or much larger than the other values in a set of data.	<p>The scatter plot shows a positive linear correlation between two variables. The x-axis ranges from 0 to 100 with major ticks every 20 units. The y-axis ranges from 0 to 12 with major ticks every 2 units. A solid black line of best fit passes through the origin and the point (100, 12). There are 10 data points plotted as blue diamonds. One point at approximately (30, 10) is significantly above the line and is labeled 'Outlier' with a red arrow pointing to it. The other points are clustered around the line of best fit.</p> <table border="1"><caption>Data points from the scatter plot</caption><thead><tr><th>X-axis value</th><th>Y-axis value</th></tr></thead><tbody><tr><td>10</td><td>2</td></tr><tr><td>20</td><td>3</td></tr><tr><td>30</td><td>10 (Outlier)</td></tr><tr><td>35</td><td>8.5</td></tr><tr><td>40</td><td>4.5</td></tr><tr><td>50</td><td>6</td></tr><tr><td>60</td><td>8</td></tr><tr><td>70</td><td>7.5</td></tr><tr><td>80</td><td>8.5</td></tr><tr><td>90</td><td>10</td></tr></tbody></table>	X-axis value	Y-axis value	10	2	20	3	30	10 (Outlier)	35	8.5	40	4.5	50	6	60	8	70	7.5	80	8.5	90	10
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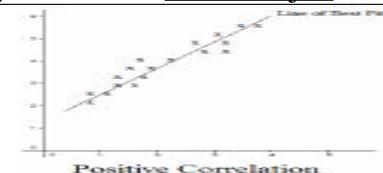
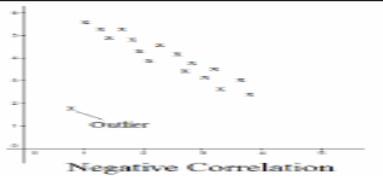
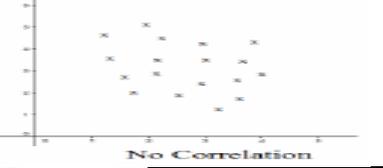
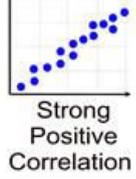
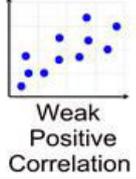
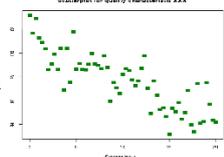
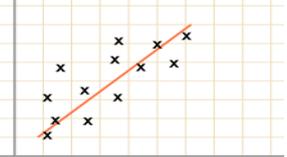
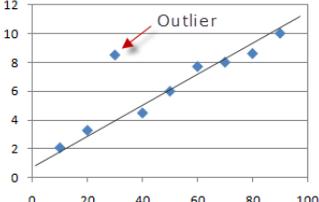


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1. Frequency Table	A record of how often each value in a set of data occurs .	<table border="1"> <thead> <tr> <th>Number of marks</th> <th>Tally marks</th> <th>Frequency</th> </tr> </thead> <tbody> <tr> <td>1</td> <td> </td> <td>7</td> </tr> <tr> <td>2</td> <td> </td> <td>5</td> </tr> <tr> <td>3</td> <td> </td> <td>6</td> </tr> <tr> <td>4</td> <td> </td> <td>5</td> </tr> <tr> <td>5</td> <td> </td> <td>3</td> </tr> <tr> <td>Total</td> <td></td> <td>26</td> </tr> </tbody> </table>	Number of marks	Tally marks	Frequency	1		7	2		5	3		6	4		5	5		3	Total		26													
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2. Bar Chart	Represents data as vertical blocks. <i>x – axis</i> shows the type of data <i>y – axis</i> shows the frequency for each type of data Each bar should be the same width There should be gaps between each bar Remember to label each axis.	<table border="1"> <caption>Data for Bar Chart</caption> <thead> <tr> <th>Number of pets owned</th> <th>Frequency</th> </tr> </thead> <tbody> <tr><td>0</td><td>3</td></tr> <tr><td>1</td><td>8</td></tr> <tr><td>2</td><td>12</td></tr> <tr><td>3</td><td>1</td></tr> <tr><td>4</td><td>2</td></tr> </tbody> </table>	Number of pets owned	Frequency	0	3	1	8	2	12	3	1	4	2																						
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3. Types of Bar Chart	<p>Compound/Composite Bar Charts show data stacked on top of each other.</p> <p>Comparative/Dual Bar Charts show data side by side.</p>	<table border="1"> <caption>Data for Compound Bar Chart</caption> <thead> <tr> <th>Sample</th> <th>Aluminum (g)</th> <th>Carbon (g)</th> <th>Iron (g)</th> </tr> </thead> <tbody> <tr><td>A</td><td>25</td><td>20</td><td>15</td></tr> <tr><td>B</td><td>20</td><td>15</td><td>10</td></tr> <tr><td>C</td><td>25</td><td>20</td><td>25</td></tr> </tbody> </table> <table border="1"> <caption>Data for Dual Bar Chart (Rainfall)</caption> <thead> <tr> <th>Month</th> <th>London (cm)</th> <th>Bristol (cm)</th> </tr> </thead> <tbody> <tr><td>Jan</td><td>15</td><td>12</td></tr> <tr><td>Feb</td><td>20</td><td>18</td></tr> <tr><td>Mar</td><td>32</td><td>30</td></tr> <tr><td>Apr</td><td>45</td><td>40</td></tr> <tr><td>May</td><td>48</td><td>45</td></tr> </tbody> </table>	Sample	Aluminum (g)	Carbon (g)	Iron (g)	A	25	20	15	B	20	15	10	C	25	20	25	Month	London (cm)	Bristol (cm)	Jan	15	12	Feb	20	18	Mar	32	30	Apr	45	40	May	48	45
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4. Pie Chart	Used for showing how data breaks down into its constituent parts . When drawing a pie chart, divide 360° by the total frequency . This will tell you how many degrees to use for the frequency of each category. Remember to label the category that each sector in the pie chart represents.	<p>If there are 40 people in a survey, then each person will be worth $360 \div 40 = 9^\circ$ of the pie chart.</p>																																		



<p>5. Pictogram</p>	<p>Uses pictures or symbols to show the value of the data.</p> <p>A pictogram must have a key.</p>	<p>Black </p> <p>Red </p> <p>Green   = 4 cars</p> <p>Others </p>																																																
<p>6. Line Graph</p>	<p>A graph that uses points connected by straight lines to show how data changes in values.</p> <p>This can be used for time series data, which is a series of data points spaced over uniform time intervals in time order.</p>																																																	
<p>7. Two Way Tables</p>	<p>A table that organises data around two categories.</p> <p>Fill out the information step by step using the information given.</p> <p>Make sure all the totals add up for all columns and rows.</p>	<p>Question: Complete the 2 way table below.</p> <table border="1" data-bbox="954 707 1422 801"> <thead> <tr> <th></th> <th>Left Handed</th> <th>Right Handed</th> <th>Total</th> </tr> </thead> <tbody> <tr> <td>Boys</td> <td>10</td> <td></td> <td>58</td> </tr> <tr> <td>Girls</td> <td></td> <td></td> <td></td> </tr> <tr> <td>Total</td> <td></td> <td>84</td> <td>100</td> </tr> </tbody> </table> <p>Answer: Step 1, fill out the easy parts (the totals)</p> <table border="1" data-bbox="954 819 1422 913"> <thead> <tr> <th></th> <th>Left Handed</th> <th>Right Handed</th> <th>Total</th> </tr> </thead> <tbody> <tr> <td>Boys</td> <td>10</td> <td>48</td> <td>58</td> </tr> <tr> <td>Girls</td> <td></td> <td></td> <td>42</td> </tr> <tr> <td>Total</td> <td>16</td> <td>84</td> <td>100</td> </tr> </tbody> </table> <p>Answer: Step 2, fill out the remaining parts</p> <table border="1" data-bbox="954 931 1422 1021"> <thead> <tr> <th></th> <th>Left Handed</th> <th>Right Handed</th> <th>Total</th> </tr> </thead> <tbody> <tr> <td>Boys</td> <td>10</td> <td>48</td> <td>58</td> </tr> <tr> <td>Girls</td> <td>6</td> <td>36</td> <td>42</td> </tr> <tr> <td>Total</td> <td>16</td> <td>84</td> <td>100</td> </tr> </tbody> </table>		Left Handed	Right Handed	Total	Boys	10		58	Girls				Total		84	100		Left Handed	Right Handed	Total	Boys	10	48	58	Girls			42	Total	16	84	100		Left Handed	Right Handed	Total	Boys	10	48	58	Girls	6	36	42	Total	16	84	100
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1. Correlation	Correlation between two sets of data means they are connected in some way.	There is correlation between temperature and the number of ice creams sold.
2. Causality	When one variable influences another variable.	The more hours you work at a particular job (paid hourly), the higher your income <u>from that job</u> will be.
3. Positive Correlation	As one value increases the other value increases .	 Positive Correlation
4. Negative Correlation	As one value increases the other value decreases .	 Negative Correlation
5. No Correlation	There is no linear relationship between the two.	 No Correlation
6. Strong Correlation	When two sets of data are closely linked .	 Strong Positive Correlation
7. Weak Correlation	When two sets of data have correlation, but are not closely linked .	 Weak Positive Correlation
8. Scatter Graph	A graph in which values of two variables are plotted along two axes to compare them and see if there is any connection between them.	
9. Line of Best Fit	A straight line that best represents the data on a scatter graph.	
10. Outlier	A value that 'lies outside' most of the other values in a set of data. An outlier is much smaller or much larger than the other values in a set of data.	

Subject: Maths



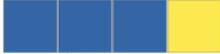
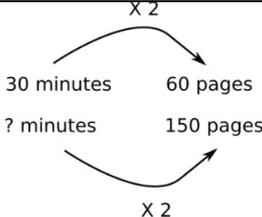


Topic/Skill	Definition/Tips	Example
1. Percentage	Number of parts per 100.	31% means $\frac{31}{100}$
2. Finding 10%	To find 10% , divide by 10	10% of £36 = $36 \div 10 = \text{£}3.60$
3. Finding 1%	To find 1% , divide by 100	1% of £8 = $8 \div 100 = \text{£}0.08$
4. Percentage Change	$\frac{\text{Difference}}{\text{Original}} \times 100\%$	A games console is bought for £200 and sold for £250. % change = $\frac{50}{200} \times 100 = 25\%$
5. Fractions to Decimals	Divide the numerator by the denominator using the bus stop method.	$\frac{3}{8} = 3 \div 8 = 0.375$
6. Decimals to Fractions	Write as a fraction over 10, 100 or 1000 and simplify.	$0.36 = \frac{36}{100} = \frac{9}{25}$
7. Percentages to Decimals	Divide by 100	$8\% = 8 \div 100 = 0.08$
8. Decimals to Percentages	Multiply by 100	$0.4 = 0.4 \times 100\% = 40\%$
9. Fractions to Percentages	Percentage is just a fraction out of 100. Make the denominator 100 using equivalent fractions. When the denominator doesn't go in to 100, use a calculator and multiply the fraction by 100.	$\frac{3}{25} = \frac{12}{100} = 12\%$ $\frac{9}{17} \times 100 = 52.9\%$
10. Percentages to Fractions	Percentage is just a fraction out of 100. Write the percentage over 100 and simplify.	$14\% = \frac{14}{100} = \frac{7}{50}$

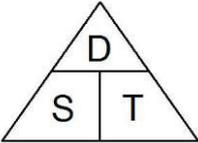
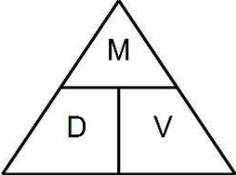


Topic/Skill	Definition/Tips	Example
1. Increase or Decrease by a Percentage	<p>Non-calculator: Find the percentage and add or subtract it from the original amount.</p> <p>Calculator: Find the percentage multiplier and multiply.</p>	<p><u>Increase 500 by 20% (Non Calc):</u> $10\% \text{ of } 500 = 50$ so $20\% \text{ of } 500 = 100$ $500 + 100 = 600$</p> <p><u>Decrease 800 by 17% (Calc):</u> $100\% - 17\% = 83\%$ $83\% \div 100 = 0.83$ $0.83 \times 800 = 664$</p>
2. Percentage Multiplier	The number you multiply a quantity by to increase or decrease it by a percentage .	<p>The multiplier for increasing by 12% is 1.12</p> <p>The multiplier for decreasing by 12% is 0.88</p> <p>The multiplier for increasing by 100% is 2.</p>
3. Reverse Percentage	<p>Find the correct percentage given in the question, then work backwards to find 100%</p> <p>Look out for words like 'before' or 'original'</p>	<p>A jumper was priced at £48.60 after a 10% reduction. Find its original price.</p> <p>$100\% - 10\% = 90\%$</p> <p>$90\% = £48.60$ $1\% = £0.54$ $100\% = £54$</p>
4. Simple Interest	Interest calculated as a percentage of the original amount.	<p>£1000 invested for 3 years at 10% simple interest.</p> <p>$10\% \text{ of } £1000 = £100$</p> <p>Interest = $3 \times £100 = £300$</p>



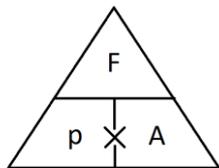
Topic/Skill	Definition/Tips	Example
1. Ratio	Ratio compares the size of one part to another part . Written using the ':' symbol.	$3 : 1$ 
2. Proportion	Proportion compares the size of one part to the size of the whole . Usually written as a fraction.	In a class with 13 boys and 9 girls, the proportion of boys is $\frac{13}{22}$ and the proportion of girls is $\frac{9}{22}$
3. Simplifying Ratios	Divide all parts of the ratio by a common factor .	$5 : 10 = 1 : 2$ (divide both by 5) $14 : 21 = 2 : 3$ (divide both by 7)
4. Ratios in the form $1 : n$ or $n : 1$	Divide both parts of the ratio by one of the numbers to make one part equal 1 .	$5 : 7 = 1 : \frac{7}{5}$ in the form $1 : n$ $5 : 7 = \frac{5}{7} : 1$ in the form $n : 1$
5. Sharing in a Ratio	1. Add the total parts of the ratio. 2. Divide the amount to be shared by this value to find the value of one part. 3. Multiply this value by each part of the ratio. Use only if you know the total .	Share £60 in the ratio $3 : 2 : 1$. $3 + 2 + 1 = 6$ $60 \div 6 = 10$ $3 \times 10 = 30, 2 \times 10 = 20, 1 \times 10 = 10$ £30 : £20 : £10
6. Proportional Reasoning	Comparing two things using multiplicative reasoning and applying this to a new situation. Identify one multiplicative link and use this to find missing quantities.	
7. Unitary Method	Finding the value of a single unit and then finding the necessary value by multiplying the single unit value.	3 cakes require 450g of sugar to make. Find how much sugar is needed to make 5 cakes. $3 \text{ cakes} = 450\text{g}$ So $1 \text{ cake} = 150\text{g}$ (\div by 3) So $5 \text{ cakes} = 750 \text{ g}$ (\times by 5)
8. Ratio already shared	Find what one part of the ratio is worth using the unitary method .	Money was shared in the ratio $3:2:5$ between Ann, Bob and Cat. Given that Bob had £16, found out the total amount of money shared. $\pounds 16 = 2 \text{ parts}$ So $\pounds 8 = 1 \text{ part}$ $3 + 2 + 5 = 10 \text{ parts}$, so $8 \times 10 = \pounds 80$
9. Best Buys	Find the unit cost by dividing the price by the quantity . The lowest number is the best value.	8 cakes for £1.28 \rightarrow 16p each (\div by 8) 13 cakes for £2.05 \rightarrow 15.8p each (\div by 13) Pack of 13 cakes is best value.



Topic/Skill	Definition/Tips	Example
1. Metric System	A system of measures based on: <ul style="list-style-type: none"> - the metre for length - the kilogram for mass - the second for time Length: mm, cm, m, km Mass: mg, g, kg Volume: ml, cl, l	$1 \text{ kilometre} = 1000 \text{ metres}$ $1 \text{ metre} = 100 \text{ centimetres}$ $1 \text{ centimetre} = 10 \text{ millimetres}$ $1 \text{ kilogram} = 1000 \text{ grams}$
2. Imperial System	A system of weights and measures originally developed in England, usually based on human quantities Length: inch, foot, yard, miles Mass: lb, ounce, stone Volume: pint, gallon	$1 \text{ lb} = 16 \text{ ounces}$ $1 \text{ foot} = 12 \text{ inches}$ $1 \text{ gallon} = 8 \text{ pints}$
3. Metric and Imperial Units	Use the unitary method to convert between metric and imperial units.	$5 \text{ miles} \approx 8 \text{ kilometres}$ $1 \text{ gallon} \approx 4.5 \text{ litres}$ $2.2 \text{ pounds} \approx 1 \text{ kilogram}$ $1 \text{ inch} = 2.5 \text{ centimetres}$
4. Speed, Distance, Time	Speed = Distance \div Time Distance = Speed \times Time Time = Distance \div Speed 	Speed = 4mph Time = 2 hours Find the Distance. $D = S \times T = 4 \times 2 = 8 \text{ miles}$
5. Density, Mass, Volume	Density = Mass \div Volume Mass = Density \times Volume Volume = Mass \div Density 	Density = 8 kg/m^3 Mass = 2000g Find the Volume. $V = M \div D = 2000 \div 8 = 250 \text{ cm}^3$
6. Pressure, Force, Area	Pressure = Force \div Area Force = Pressure \times Area Area = Force \div Pressure	Pressure = 10 Pascals Area = 6 cm^2 Find the Force



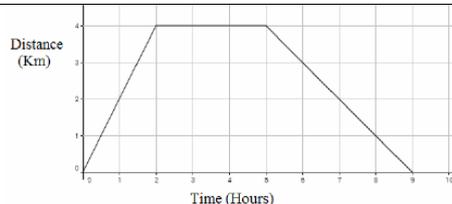
$$F = P \times A = 10 \times 6 = 60 \text{ N}$$



Remember the correct units.

7. Distance-Time Graphs

You can find the **speed** from the **gradient** of the line (Distance \div Time)
The steeper the line, the quicker the speed.
A **horizontal** line means the object is not moving (**stationary**).

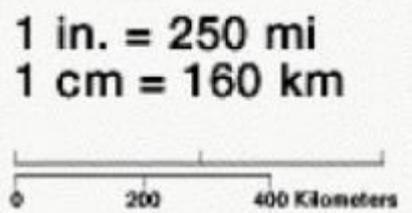
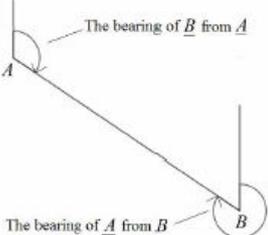
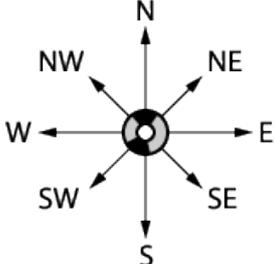




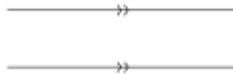
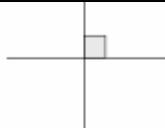
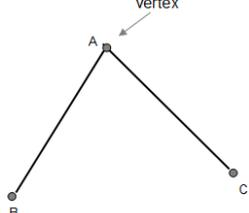
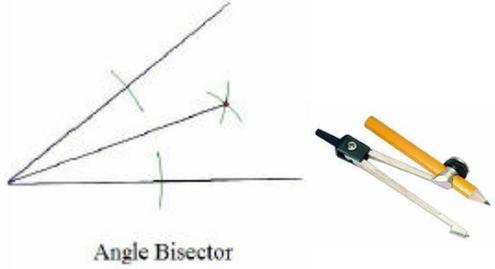
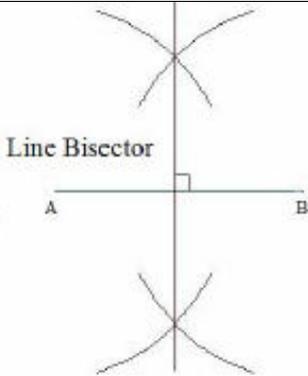
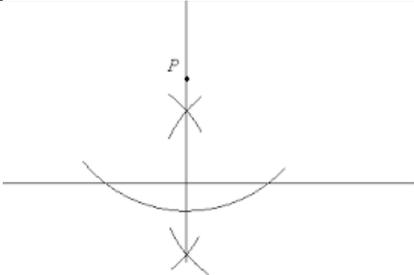
Topic/Skill	Definition/Tips	Example
1. Translation	<p>Translate means to move a shape. The shape does not change size or orientation.</p>	
2. Column Vector	<p>In a column vector, the top number moves left (-) or right (+) and the bottom number moves up (+) or down (-)</p>	<p>$\begin{pmatrix} 2 \\ 3 \end{pmatrix}$ means '2 right, 3 up' $\begin{pmatrix} -1 \\ -5 \end{pmatrix}$ means '1 left, 5 down'</p>
3. Rotation	<p>The size does not change, but the shape is turned around a point. Use tracing paper.</p>	<p>Rotate Shape A 90° anti-clockwise about (0,1)</p>
4. Reflection	<p>The size does not change, but the shape is 'flipped' like in a mirror.</p> <p>Line $x = ?$ is a vertical line. Line $y = ?$ is a horizontal line. Line $y = x$ is a diagonal line.</p>	<p>Reflect shape C in the line $y = x$</p>
5. Enlargement	<p>The shape will get bigger or smaller. Multiply each side by the scale factor.</p>	<p>Scale Factor = 3 means '3 times larger = multiply by 3' Scale Factor = $\frac{1}{2}$ means 'half the size = divide by 2'</p>

<p>6. Finding the Centre of Enlargement</p>	<p>Draw straight lines through corresponding corners of the two shapes. The centre of enlargement is the point where all the lines cross over.</p> <p>Be careful with negative enlargements as the corresponding corners will be the other way around.</p>	<p>A to B is an enlargement SF 2 about the point (2,1)</p>
<p>7. Describing Transformations</p>	<p>Give the following information when describing each transformation:</p> <p>Look at the number of marks in the question for a hint of how many pieces of information are needed.</p> <p>If you are asked to describe a 'transformation', you need to say the name of the type of transformation as well as the other details.</p>	<ul style="list-style-type: none"> - Translation, Vector - Rotation, Direction, Angle, Centre - Reflection, Equation of mirror line - Enlargement, Scale factor, Centre of enlargement
<p>8. Negative Scale Factor Enlargements</p>	<p>Negative enlargements will look like they have been rotated.</p> <p>$SF = -2$ will be rotated, and also twice as big.</p>	<p>Enlarge ABC by scale factor -2, centre (1,1)</p>
<p>9. Invariance</p>	<p>A point, line or shape is invariant if it does not change/move when a transformation is performed.</p> <p>An invariant point 'does not vary'.</p>	<p>If shape P is reflected in the $y - axis$, then exactly one vertex is invariant.</p>



Topic/Skill	Definition/Tips	Example
1. Scale	The ratio of the length in a model to the length of the real thing.	 <p>Real Horse 1500 mm high 2000 mm long</p> <p>Drawn Horse 150 mm high 200 mm long</p>
2. Scale (Map)	The ratio of a distance on the map to the actual distance in real life .	 <p>1 in. = 250 mi 1 cm = 160 km</p> <p>0 200 400 Kilometers</p>
3. Bearings	<p>1. Measure from North (draw a North line)</p> <p>2. Measure clockwise</p> <p>3. Your answer must have 3 digits (eg. 047°)</p> <p>Look out for where the bearing is measured <u>from</u>.</p>	
4. Compass Directions	<p>You can use an acronym such as 'Never Eat Shredded Wheat' to remember the order of the compass directions in a clockwise direction.</p> <p>Bearings: <i>NE = 045°, W = 270° etc.</i></p>	



Topic/Skill	Definition/Tips	Example
1. Parallel	Parallel lines never meet.	
2. Perpendicular	Perpendicular lines are at right angles. There is a 90° angle between them.	
3. Vertex	A corner or a point where two lines meet.	
4. Angle Bisector	<p>Angle Bisector: Cuts the angle in half.</p> <ol style="list-style-type: none"> 1. Place the sharp end of a pair of compasses on the vertex. 2. Draw an arc, marking a point on each line. 3. Without changing the compass put the compass on each point and mark a centre point where two arcs cross over. 4. Use a ruler to draw a line through the vertex and centre point. 	 <p style="text-align: center;">Angle Bisector</p>
5. Perpendicular Bisector	<p>Perpendicular Bisector: Cuts a line in half and at right angles.</p> <ol style="list-style-type: none"> 1. Put the sharp point of a pair of compasses on A. 2. Open the compass over half way on the line. 3. Draw an arc above and below the line. 4. Without changing the compass, repeat from point B. 5. Draw a straight line through the two intersecting arcs. 	 <p style="text-align: center;">Line Bisector</p>
6. Perpendicular from an External Point	<p>The perpendicular distance from a point to a line is the shortest distance to that line.</p> <ol style="list-style-type: none"> 1. Put the sharp point of a pair of compasses on the point. 2. Draw an arc that crosses the line twice. 3. Place the sharp point of the compass on one of these points, open over half way and draw an arc above and below the line. 4. Repeat from the other point on the line. 	



	5. Draw a straight line through the two intersecting arcs.	
7. Perpendicular from a Point on a Line	<p>Given line PQ and point R on the line:</p> <ol style="list-style-type: none"> 1. Put the sharp point of a pair of compasses on point R. 2. Draw two arcs either side of the point of equal width (giving points S and T) 3. Place the compass on point S, open over halfway and draw an arc above the line. 4. Repeat from the other arc on the line (point T). 5. Draw a straight line from the intersecting arcs to the original point on the line. 	
8. Constructing Triangles (Side, Side, Side)	<ol style="list-style-type: none"> 1. Draw the base of the triangle using a ruler. 2. Open a pair of compasses to the width of one side of the triangle. 3. Place the point on one end of the line and draw an arc. 4. Repeat for the other side of the triangle at the other end of the line. 5. Using a ruler, draw lines connecting the ends of the base of the triangle to the point where the arcs intersect. 	
9. Constructing Triangles (Side, Angle, Side)	<ol style="list-style-type: none"> 1. Draw the base of the triangle using a ruler. 2. Measure the angle required using a protractor and mark this angle. 3. Remove the protractor and draw a line of the exact length required in line with the angle mark drawn. 4. Connect the end of this line to the other end of the base of the triangle. 	
10. Constructing Triangles (Angle, Side, Angle)	<ol style="list-style-type: none"> 1. Draw the base of the triangle using a ruler. 2. Measure one of the angles required using a protractor and mark this angle. 3. Draw a straight line through this point from the same point on the base of the triangle. 4. Repeat this for the other angle on the other end of the base of the triangle. 	

<p>11. Constructing an Equilateral Triangle (also makes a 60° angle)</p>	<ol style="list-style-type: none"> 1. Draw the base of the triangle using a ruler. 2. Open the pair of compasses to the exact length of the side of the triangle. 3. Place the sharp point on one end of the line and draw an arc. 4. Repeat this from the other end of the line. 5. Using a ruler, draw lines connecting the ends of the base to the point where the arcs intersect. 	
<p>12. Loci and Regions</p>	<p>A locus is a path of points that follow a rule.</p> <p>For the locus of points closer to B than A, create a perpendicular bisector between A and B and shade the side closer to B.</p> <p>For the locus of points equidistant from A, use a compass to draw a circle, centre A.</p> <p>For the locus of points equidistant to line X and line Y, create an angle bisector.</p> <p>For the locus of points a set distance from a line, create two semi-circles at either end joined by two parallel lines.</p>	
<p>13. Equidistant</p>	<p>A point is equidistant from a set of objects if the distances between that point and each of the objects is the same.</p>	